



# Lubricant properties of a polyalphaolefin oil additivated with zirconia and ceria-zirconia nanoparticles

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## ARTICLE INFO

### Keywords:

Zirconia  
Ceria-zirconia  
Polyalphaolefin  
Viscosity  
Friction coefficient  
Wear

## ABSTRACT

In this work zirconia ( $ZrO_2$ ) and hybrid ceria-zirconia ( $CeO_2-ZrO_2$ ) nanoparticles are used for the first time as lubricant additives of the PAO8 base oil (low-viscosity polyalphaolefin oil) at concentrations from 0.05 wt% to 0.20 wt%. Thermophysical properties of the eight formulated nanolubricants were experimentally determined observing that the presence of these nanoadditives not significantly alter the volumetric behaviour of neat PAO8. On the contrary, the presence of  $CeO_2-ZrO_2$  in formulation increases the viscosity of the base oil by up to 13%. Tribological tests were performed under pure sliding conditions at 393.15 K at a load of 20 N using a ball-on-three-pin rotational tribometer. Moreover, the wear was quantified with a 3D optical profilometer. Nanolubricants with zirconia nanoparticles exhibited superior characteristics in terms of stability, antifriction and anti-wear properties than those formulated with hybrid ceria-zirconia nanoparticles. The best tribological behaviour was obtained with 0.05 wt%  $ZrO_2$ , thus reductions of 13 % in friction coefficient and of 73 % in the worn area were obtained. The results obtained have been compared with those previously reported for the same base oil (PAO8) and other types of nanoadditives. Finally, surface roughness analysis, Raman microscopy and SEM-EDX were used to analyse the wear mechanism produced by zirconia and hybrid ceria-zirconia nanoparticles.

## 1. Introduction

Electric vehicles (EVs) offer a sustainable and eco-friendly alternative to internal combustion vehicles, but their operating conditions—high speeds, heavy loads, elevated temperatures, and electrical currents—place unique demands on their mechanical components (e.g., motors, transmissions, wheel bearings, and suspensions) [1–3]. Consequently, minimizing friction in electric drivetrains is crucial to enhance efficiency and achieve energy savings.

The development of transmission fluids for EVs involves close collaboration among lubricant manufacturers, automotive engineers, and researchers. Advances in lubricant technology not only improve overall vehicle efficiency and reliability but also ensure compatibility with the specific materials used in EV components (seals, gaskets, various metals) while providing necessary electrical insulation, thermal stability, and low viscosity to reduce motor torque and enhance cooling performance [2–7]. Lubricants typically comprise 80–90 % base oil and

10–20 % additives, so carefully selecting both components is essential to meet these diverse performance requirements. In response to growing environmental concerns associated with petroleum-derived products, synthetic base oils—particularly polyalphaolefins (PAOs)—have become prevalent due to their high thermal stability, oxidation resistance, and dielectric properties. PAOs are classified by their kinematic viscosities at 373.15 K, typically ranging from 2 to 100 cSt [8,9].

Recent studies have demonstrated that incorporating nanomaterials into PAOs can significantly enhance their tribological properties by mechanisms such as rolling effects, protective film formation, repair, and polishing [10–13]. Most of the published work in this area has focused on metal-containing nanomaterials, including their oxides and sulphides [13–15]. For instance, Kalin et al. [16] showed that PAO6 additivated with  $MoS_2$  multi-wall nanotubes reduced friction and wear by up to 2 and 9 times, respectively, compared to neat PAO6. Other studies have similarly reported significant improvements using  $WS_2$ , Ni, ZnO, and other nanoparticles [12,17–23].

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<https://doi.org/10.1016/j.molliq.2025.127502>

Received 25 November 2024; Received in revised form 13 March 2025; Accepted 1 April 2025

Available online 2 April 2025

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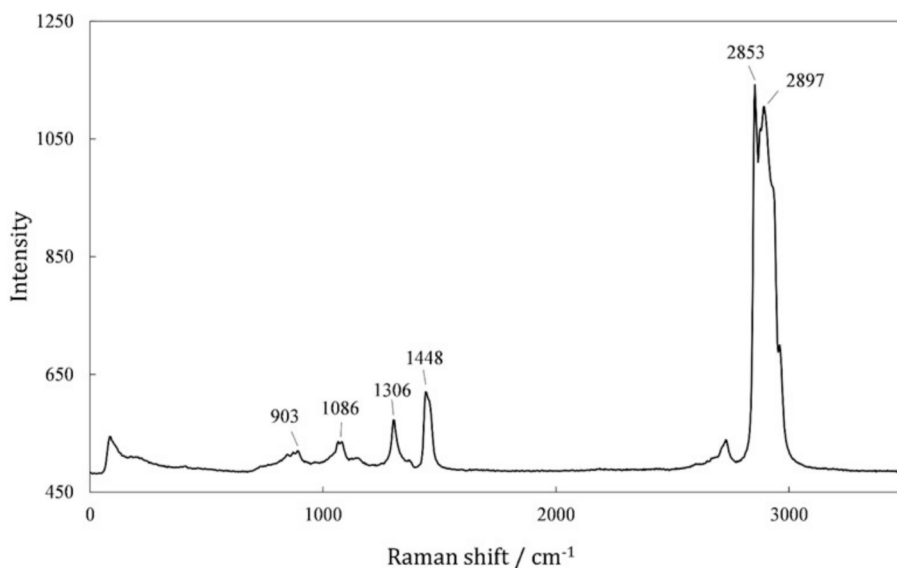


Fig. 1. Raman spectrum of PAO8 base oil.

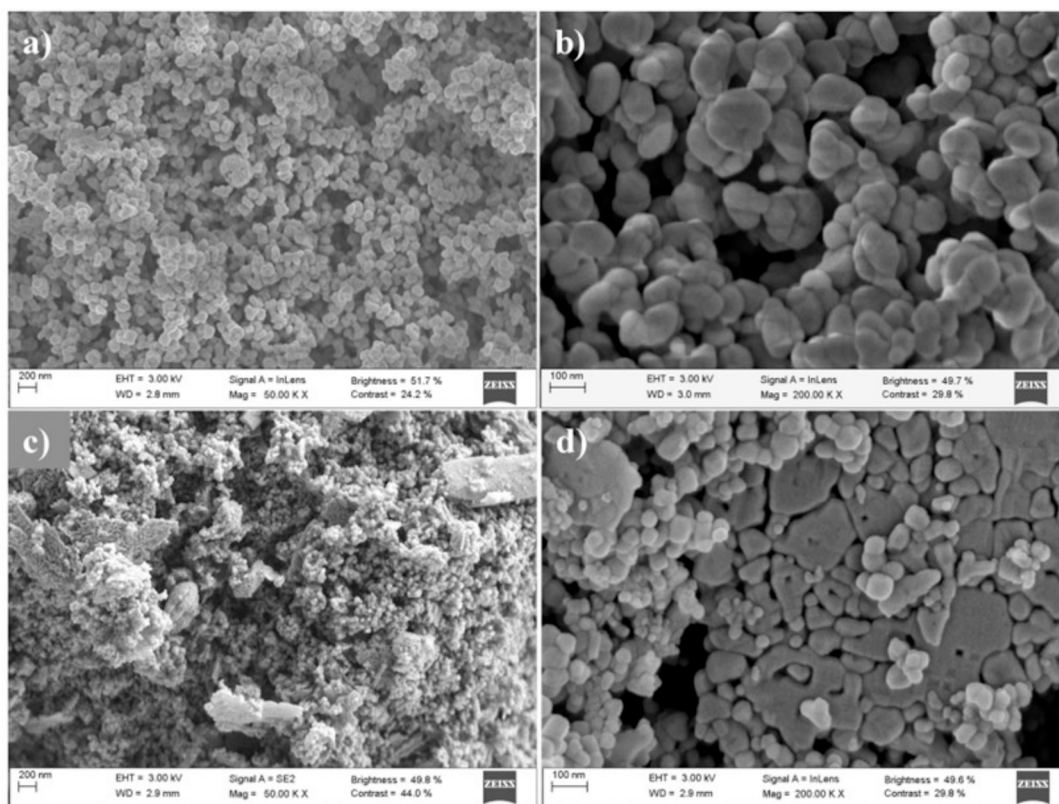


Fig. 2. SEM images of  $ZrO_2$  at a) 50 K X and b) 200 K X and  $CeO_2-ZrO_2$  at c) 50 K X and d) 200 K X.

Within this context, the present study is part of a broader research project focused on the thermophysical and tribological properties of nanolubricants for EVs. For transmission fluids in EVs, low-viscosity base oils are essential; thus, we have selected PAO8 (kinematic viscosity around  $8 \text{ mm}^2/\text{s}$  at  $373.15 \text{ K}$ ). While previous works have explored the effects of  $ZrO_2$  nanoparticles in PAO6 and PAO4 [6,24–27], there is a notable gap regarding the use of  $CeO_2/ZrO_2$  hybrid nanoparticles in PAO formulations. Only Philip et al. [28] have examined the surface morphology of  $CeO_2$  and Ce-Zr hybrid nanoparticles for potential lubricant applications, and studies on  $CeO_2$  as an additive in PAOs have

indicated that  $CeO_2$ -based composites can enhance tribological performance [29–31].

The novelty of our work lies in the first-time use of  $ZrO_2$  and  $CeO_2/ZrO_2$  hybrid nanoparticles as additives in PAO8. This study aims to complete the evaluation of various nanomaterials as additives in poly-alphaolefins, potentially leading to optimized formulations that offer superior performance in EV transmission systems.

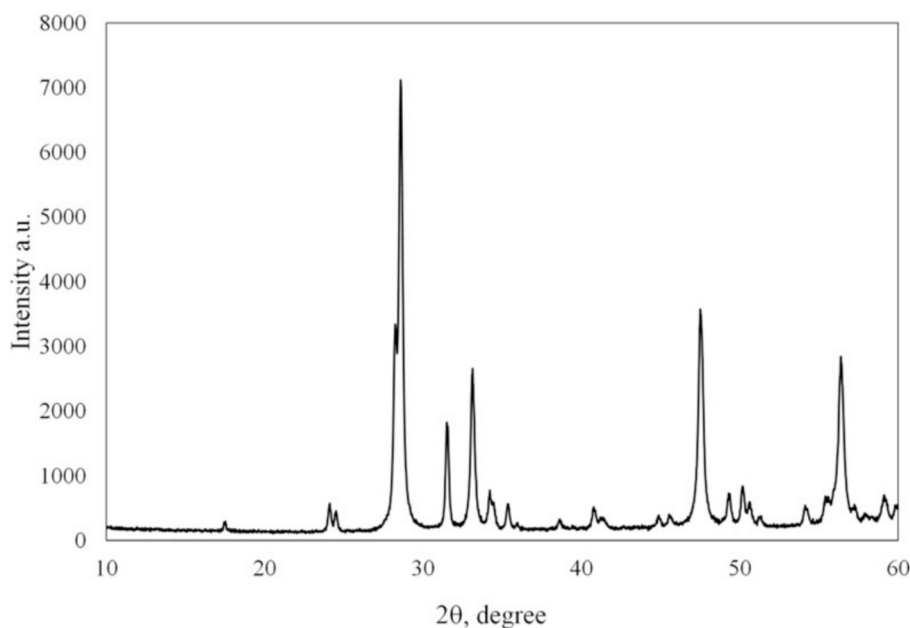


Fig. 3. X-ray patterns of the nanopowder of  $\text{CeO}_2\text{-ZrO}_2$ .

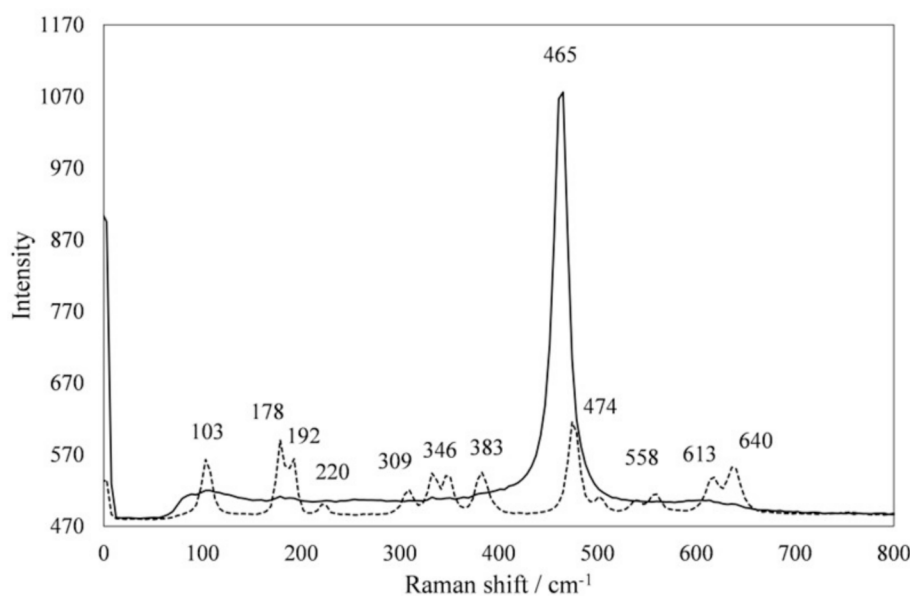


Fig. 4. Raman spectra of  $\text{ZrO}_2$  (dashed line) and  $\text{CeO}_2\text{-ZrO}_2$  (solid line).

## 2. Materials

### 2.1. Nanoadditives and base oil characterisation

A low viscosity polyalphaolefin (PAO8) supplied by Repsol, with a viscosity index of 138, was used as base oil to prepare the nano-lubricants. Density and viscosity of PAO8 over the temperature interval 278.15 to 373.15 K are reported in Tables S1 and S2 in the Supplementary Material. PAO8 dynamic viscosity ranges from 6.26 to 253.14 mPa s and density from 0.7794 to 0.8375  $\text{g cm}^{-3}$ , over all the temperature intervals. Raman spectrum of PAO8 oil, shown in Fig. 1, was performed with a WITec alpha300R+ confocal Raman microscopy at a wavelength of 532 nm. An intense broad band was detected around 2800–3000  $\text{cm}^{-1}$  with peaks at 2853 and 2897  $\text{cm}^{-1}$  assignable to C–H stretching [32]. The peaks at 1306 and 1448  $\text{cm}^{-1}$  correspond to the

$\delta(\text{CH}_2)$  and  $\delta(\text{CH}_3)$  vibrations, respectively [32], and the peaks at 903 and 1086  $\text{cm}^{-1}$  can be attributed to the vibrations of the aliphatic  $\nu(\text{C}-\text{C})$  chains [33].

$\text{ZrO}_2$  nanoparticles (Iolitec) and  $\text{CeO}_2\text{-ZrO}_2$  nanocomposite (US Research Nanomaterials, Inc.) were used as lubricant additives. The size and morphology of  $\text{ZrO}_2$  and  $\text{CeO}_2\text{-ZrO}_2$  nanopowders were analysed by scanning electron microscopy (SEM). As shown in Fig. 2, SEM images reveal that the two types of nanoparticles have a spherical shape and the difference in size between  $\text{ZrO}_2$  (30–60 nm) and  $\text{CeO}_2\text{-ZrO}_2$  (15 nm) can be distinguished. The X-ray patterns of  $\text{ZrO}_2$  nanopowder is reported in a previous work [24]. EDX spectrum and elemental mapping of  $\text{CeO}_2\text{-ZrO}_2$  nanoadditives are shown in Fig. S1 in the Supplementary Material. Elemental mapping (Fig. S1 a, b and c) reveals a homogeneous distribution on the nanoadditives. In particular, the distribution of elements: Ce, O and Zr, was 27.7, 20.2 and 14.1 wt%, respectively. As can be seen

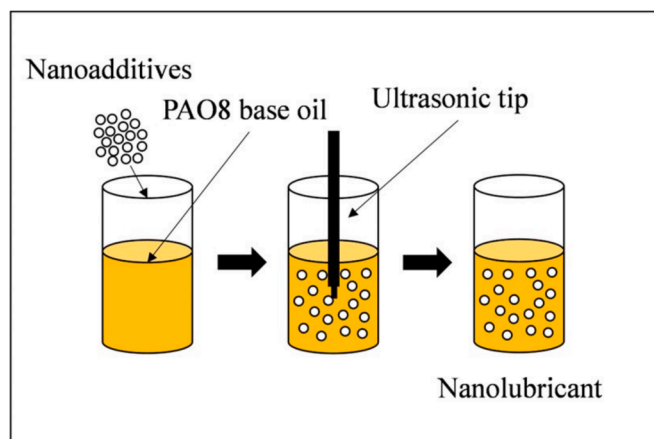


Fig. 5. Scheme of the procedure used for the nanolubricants formulation.

from Fig. 3, the main phase of  $\text{CeO}_2\text{-ZrO}_2$  nanopowders is the typical diffraction peaks of  $\text{Ce}_{0.02}\text{O}_2\text{Zr}_{0.98}$  cubic phase at  $2\theta = 28.57^\circ$ ,  $33.10^\circ$ ,  $47.50^\circ$ , and  $56.36^\circ$  due to (111), (200), (220) and (311) planes, respectively [34].

To complete the characterisation of the nanopowders, Raman spectroscopy was employed using the confocal Raman microscope (WITec alpha300R+) with a 532 nm excitation laser. Fig. 4 shows the Raman spectra with the characteristic bands for both nanoparticles. In the  $\text{ZrO}_2$  spectrum, several peaks are observed centred at 103, 178, 192, 309, 346, 383, 474, 558, 618 and  $640\text{ cm}^{-1}$ . The peaks of highest intensity are placed at 103, 178 and  $474\text{ cm}^{-1}$ , which confirm the monoclinic crystal structure of  $\text{ZrO}_2$  nanoparticles [35]. In the case of the Raman spectrum of  $\text{CeO}_2\text{-ZrO}_2$  hybrid nanoparticles, characteristic bands are observed around 103, 465 and  $618\text{ cm}^{-1}$ . The strongest peak at  $465\text{ cm}^{-1}$  corresponds to cerium oxide [36], while the weak peaks at 103 and  $618\text{ cm}^{-1}$  are due to  $\text{ZrO}_2$ .

## 2.2. Nanolubricants preparation

Eight PAO8-based nanolubricants were prepared, four of them with  $\text{ZrO}_2$  and four with  $\text{CeO}_2\text{-ZrO}_2$  hybrid nanoparticles, in both cases the

nanoadditive mass concentrations were 0.05, 0.075, 0.10 and 0.20 wt% (Fig. 5). The addition of the powdered nanoadditives to the poly-alphaolefin oil base was controlled with a Sartorius MC 210P microbalance. To ensure the homogenisation of nanoadditives, a Bandelin Sonopuls HD2200 ultrasonic tip was used at fixed power (15 %) and frequency (37 kHz) for 30 min. An ice-water bath was used to avoid overheating of nanolubricants during the sonication process.

## 3. Experimental techniques

Density and dynamic viscosity of the nanolubricants were measured from 278.15 to 373.15 K with 5 K step, at atmospheric pressure with a rotational Stabinger viscometer SVM 3000 from Anton Paar (Graz, Austria). The automated viscometer is based on a modified Couette principle, which includes a vibrating tube densimeter. In addition, this equipment was also used to determine the viscosity index (VI) according to ASTM D2270 and ISO 2909 standards. This device has previously been described in detail [37]. The expanded uncertainties ( $k = 2$ ) are  $0.0005\text{ g}\cdot\text{cm}^{-3}$  and 1 % for density and dynamic viscosity, respectively. For the temperature in the range from 288.15 to 378.15 K the expanded uncertainty is 0.02 K and outside this range 0.05 K.

An Anton Paar MCR 302 rheometer equipped with a T-PTD 200 tribology cell heated by a Peltier hood HPTD200 was used to experimentally determine the friction coefficient. The test consists in a pure-sliding rotational motion between a diameter 12.7 mm ball and 6 mm three pins, with a maximum contact pressure of 1.1 GPa. The friction tests last approximately one hour. The test scheme and the conditions are shown in Fig. 6. The specimens used were polished AISI 52100 (100Cr6) steel ( $R_a = 20\text{ nm}$  for the ball and  $R_a = 50\text{ nm}$  for the pins) with hardness of 62–66 HRC. Balls and pins were cleaned with a stream of hexane and dried with air before the tests. Samples were fully submerged by adding around 1 mL of lubricant. The contact pressure and the very low surface separation are typical of the severe boundary lubrication met in automotive applications, such as gears or bearings [2,38].

To analyse the wear produced on the pins lubricated with the neat PAO8 and with the PAO8/ $\text{ZrO}_2$  and PAO8/ $\text{CeO}_2\text{-ZrO}_2$  nanolubricants a Sensofar S Neox 3D optical profilometer was used. Specifically, the following wear parameters were determined: diameter (WSD), depth, (WTD), area (A) and volume (V) of the wear track (Fig. 7). The

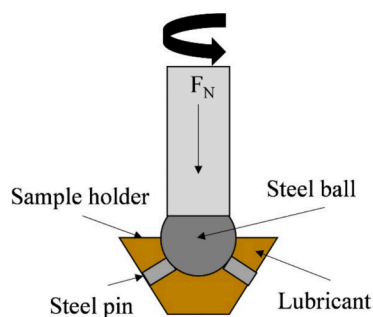


Fig. 6. Tribological test scheme and experimental conditions.

Experimental conditions	
Load (N)	20
Maximum contact pressure (GPa)	1.1
Sliding speed ( $\text{m s}^{-1}$ )	0.1
Sliding distance (m)	340
Temperature (K)	393.15

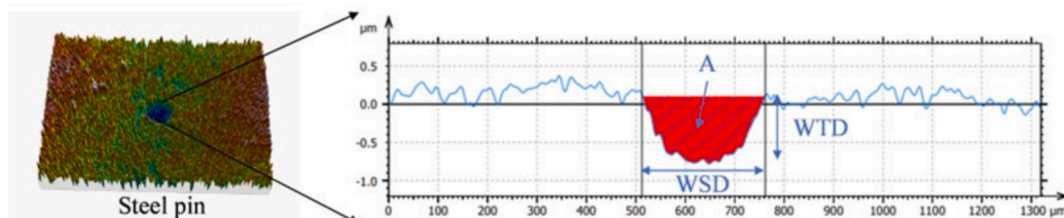


Fig. 7. Wear parameters measured using a Sensofar S Neox 3D optical profilometer.

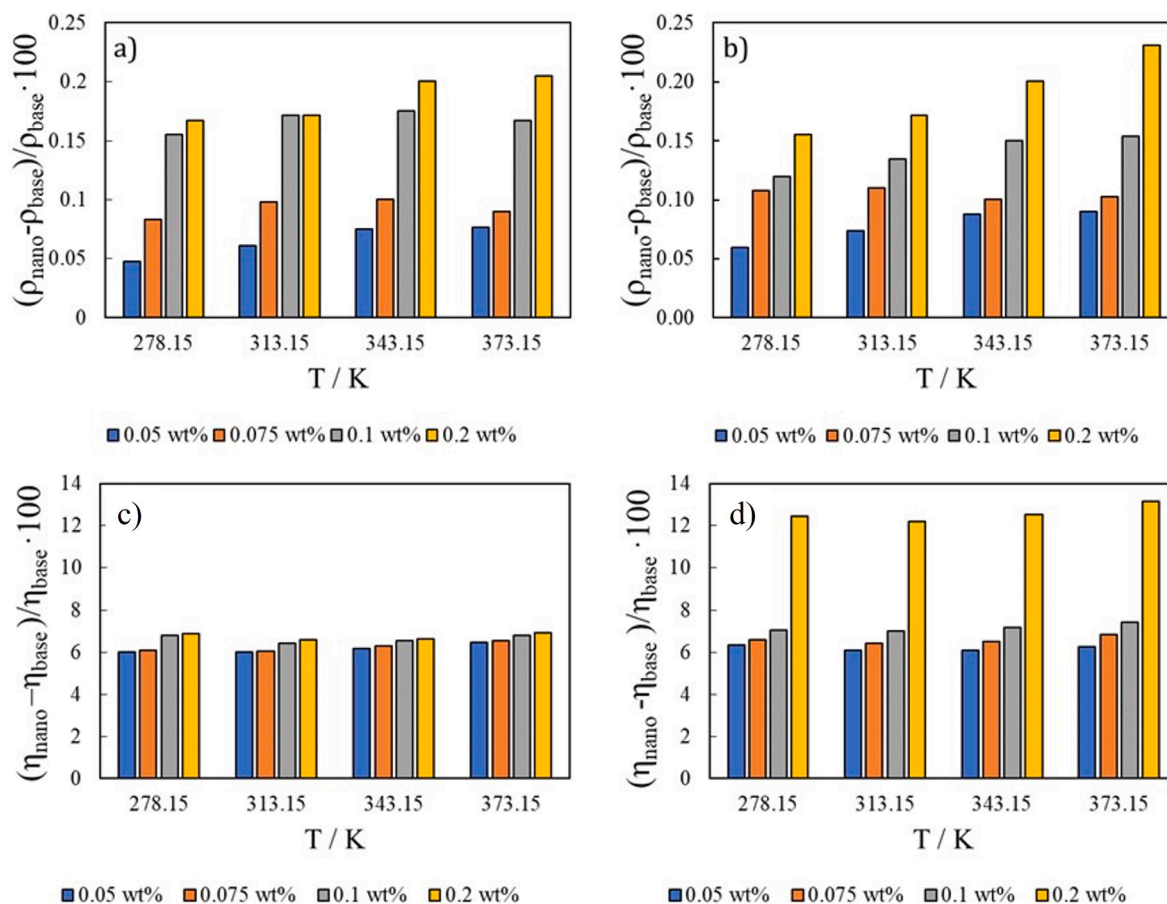


Fig. 8. Density ( $\rho$ ) and dynamic viscosity ( $\eta$ ) variation of the nanolubricants due to the presence of ZrO<sub>2</sub> (a, c) and CeO<sub>2</sub>-ZrO<sub>2</sub> (b, d) nanoparticles.

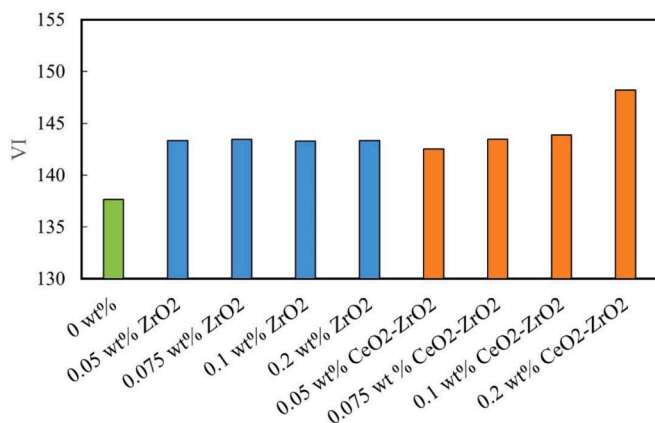


Fig. 9. Viscosity index (VI) values for PAO8 base oil (0 wt%) [23] and for all nanolubricants.

measurements were performed using the confocal mode of the optical profilometer with a 10X objective. In addition, the roughness (Ra) of the worn area of the pins was also determined and compared with the roughness of the unworn samples according to ISO4287 (Gaussian filter

with a cut-off wavelength of 0.08 mm). This analysis is useful to describe the possible anti-wear mechanism of nanoadditives. To complete the anti-wear analysis of the nanolubricants, Raman mapping of the worn surfaces was performed with the WITec alpha300R+ confocal equipment, which provides information on the distribution of the nanolubricant components (PAO8, and ZrO<sub>2</sub> or CeO<sub>2</sub>-ZrO<sub>2</sub> nanoparticles) in the wear tracks, and on the possible tribological mechanisms that can occur. To further analyze the effect of the additives in the worn pin surfaces, SEM micrographs of the PAO8 base oil and its formulated lubricants (PAO8 + 0.05 wt% ZrO<sub>2</sub> and PAO8 + 0.1 wt% CeO<sub>2</sub>-ZrO<sub>2</sub>) were obtained with a Zeiss Ultraplus Field Emission Scanning Electron Microscope, FESEM, at two magnifications (500X and 5000X).

#### 4. Results and discussion

The density values obtained for the PAO8 neat oil and for all the PAO8/ZrO<sub>2</sub> and PAO8/CeO<sub>2</sub>-ZrO<sub>2</sub> nanolubricants are presented in Table S1 in the Supplementary Material. Fig. 8a and 8b shows the density variation with the concentration for both ZrO<sub>2</sub> and CeO<sub>2</sub>-ZrO<sub>2</sub>-based nanolubricants. As can be observed, the presence of ZrO<sub>2</sub> or CeO<sub>2</sub>-ZrO<sub>2</sub> nanoparticles not significantly alter the volumetric behaviour of the neat base oil (PAO8). Thus, density relative variations less than 0.3 % are observed with the two types of nanoparticles. This fact agrees with

**Table 1**

Average friction coefficients (COF), diameter (WSD), depth (WTD) and area (A) of the worn tracks lubricated with neat PAO8, PAO8/ZrO<sub>2</sub> and PAO8/CeO<sub>2</sub>-ZrO<sub>2</sub> nanolubricants and their standard deviations ( $\sigma$ ).

Lubricant	COF	$\sigma$	WSD/ $\mu\text{m}$	$\sigma / \mu\text{m}$	WTD/ $\mu\text{m}$	$\sigma / \mu\text{m}$	A/ $10^2 \mu\text{m}^2$	$\sigma / 10^2 \mu\text{m}^2$
PAO8 [22]	0.1392	0.0021	392	14	2.35	0.17	6.05	0.52
+0.05 wt% ZrO <sub>2</sub>	0.1212	0.0021	248	9	0.81	0.15	1.46	0.36
+0.075 wt% ZrO <sub>2</sub>	0.1224	0.0025	272	10	1.01	0.10	2.45	0.49
+0.1 wt% ZrO <sub>2</sub>	0.1296	0.0026	296	5	1.44	0.09	3.27	0.24
+0.2 wt% ZrO <sub>2</sub>	0.1404	0.0038	373	3	1.89	0.10	5.08	0.22
+0.05 wt% CeO <sub>2</sub> -ZrO <sub>2</sub>	0.1345	0.0037	387	5	2.11	0.21	6.37	0.62
+0.075 wt% CeO <sub>2</sub> -ZrO <sub>2</sub>	0.1218	0.0025	302	15	1.14	0.19	2.97	0.67
+0.1 wt% CeO <sub>2</sub> -ZrO <sub>2</sub>	0.1314	0.0024	270	15	1.13	0.26	2.31	0.41
+0.2 wt% CeO <sub>2</sub> -ZrO <sub>2</sub>	0.1471	0.0040	381	14	2.16	0.32	6.30	0.95

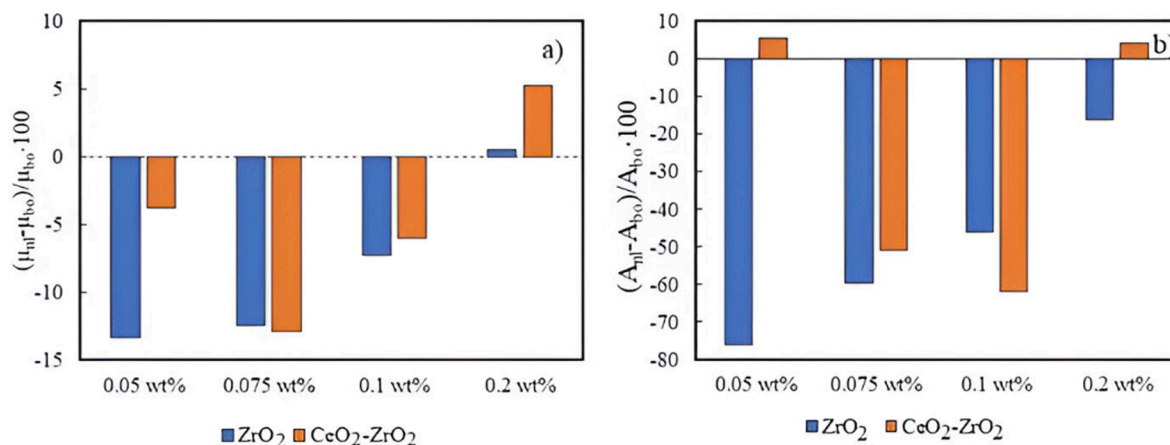


Fig. 10. Relative variation of the friction coefficient (a) and wear area (b) of nanolubricants with respect to the base oil as a function of nanoparticle concentration.

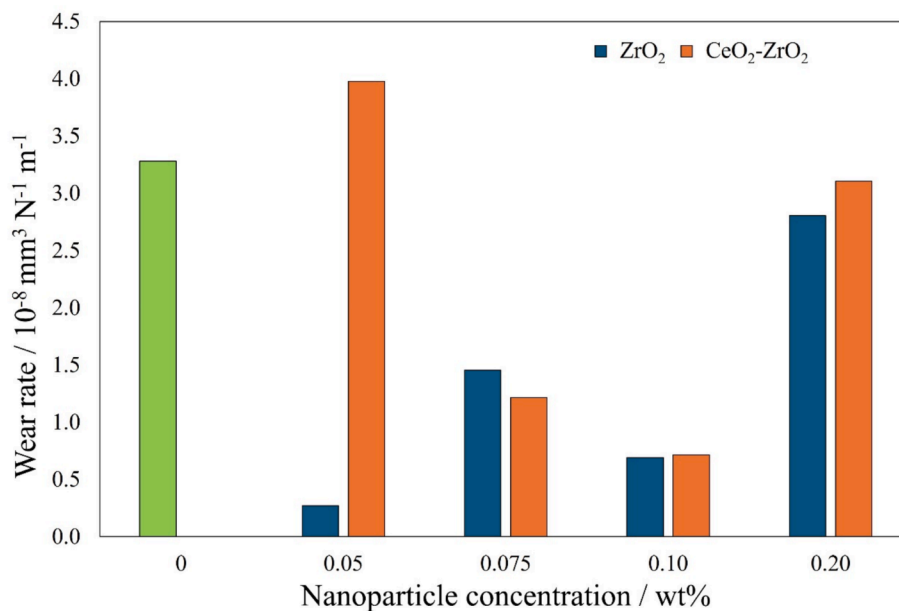


Fig. 11. Steel pins' wear rate (W) lubricated with PAO8 (0 wt%) and nanolubricants containing ZrO<sub>2</sub> and CeO<sub>2</sub>-ZrO<sub>2</sub> at different concentrations (0.05, 0.075, 0.10, and 0.20 wt%).

previous results for PAO40/ZnO-OA [21].

Table S2 gathered the dynamic viscosity values for all nanolubricants as a function of the temperature and nanoparticle concentration. As can be seen in Fig. 8c and 8d, a 0.2 wt% of CeO<sub>2</sub>-ZrO<sub>2</sub> produce an increase in the viscosity of around 13 % with respect to the neat PAO8. For the other concentrations of CeO<sub>2</sub>-ZrO<sub>2</sub> and for all PAO8/ZrO<sub>2</sub> nanolubricants, the

increase in viscosity is in the range of 6–8 %. The viscosity increase due to the presence of the nanoparticles is important for the industrial use of the nanolubricant, as it could lead to an increase in the machine's energy consumption [39]. In the case of EVs, low viscosity means higher fluidity which facilitates oil supply to the contact zone and dissipates heat by reducing viscous heating at high rpm [2].

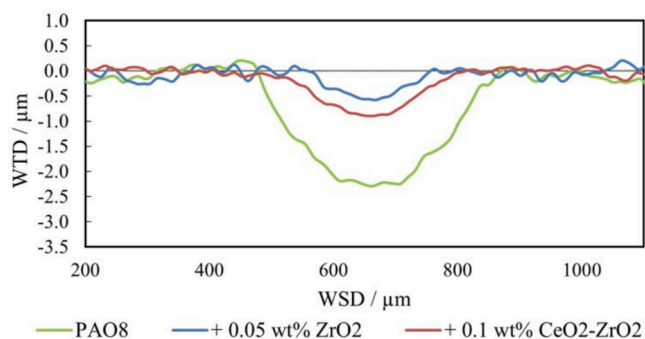


Fig. 12. Cross-sectional wear profile for base oil and for optimal nanoparticle concentrations.

As Fig. 9 shows, the presence of  $ZrO_2$  nanoparticles increases the VI from 138 (neat PAO8) to 143 (for all the  $ZrO_2$  concentrations), which means an increase of 4 %. When  $CeO_2-ZrO_2$  nanoparticles are used, we also observe values of 143–144 (for concentrations from 0.05 to 0.1 wt %) and a higher value of 148 (for the 0.2 wt % concentration). Thus, it can be concluded that the presence of the  $ZrO_2$  and  $CeO_2-ZrO_2$  nanoparticles slightly modifies the viscosity behaviour of the neat PAO8 with temperature.

The results of the friction tests and wear analysis carried out with the tribological cell T-PTD 200 and with the Sensofar S Neox 3D optical profilometer, respectively, for PAO8/ $ZrO_2$  and PAO8/ $CeO_2-ZrO_2$  at concentrations of 0.05, 0.075, 0.1 and 0.2 wt %, are shown in Table 1. As can be seen in Fig. 10a the best anti-friction (AF) behaviour occurs with the nanolubricants of PAO8 + 0.05 wt %  $ZrO_2$  and PAO8 + 0.075 wt %  $CeO_2-ZrO_2$  with an average friction coefficient value of 0.1212 and 0.1218, respectively. We must remark that a value of 0.1392 has been found for the neat PAO8 in previous works [22]. Therefore, it is observed that the presence of nanoparticles results in a reduction of the friction coefficient of around 13 % for the optimal concentrations of  $ZrO_2$  and  $CeO_2-ZrO_2$ . In general,  $ZrO_2$  nanolubricants show better AF behaviour than  $CeO_2-ZrO_2$  nanolubricants. It is important to mention that for concentrations of 0.2 wt % of the two nanoparticles the friction between the ball and the pins is higher than for the neat base oil. This fact may be due to nanoparticles agglomeration when exceeding the optimum concentration. Thus, the mechanical entrapment theory of Chiñas and Spikes [40], states that nanoparticles with a size smaller than or similar to the film thickness of the lubricant, penetrate the contact zone and deposit on it.

Regarding the anti-wear capacity (AW), the results obtained on the worn pins after contact with the ball (Table 1) show that the dispersions of  $ZrO_2$  have a greater influence in improving the anti-wear resistance of PAO8 than those of  $CeO_2-ZrO_2$ . Fig. 10b reveals the highest AW capacity of PAO8 + 0.05 wt %  $ZrO_2$ , achieving almost 76 % less worn area. It is important to note that for  $CeO_2-ZrO_2$  nanoparticles, the concentration of 0.1 wt % is the one with the greatest (around 60 % of reduction) anti-wear capacity (Fig. 10b).

The wear rate was determined from the wear volume measurements obtained from the steel pins using the following equation [41,42]:

$$W = \frac{\Delta V}{F_n S} \quad (1)$$

where  $W$  is the specific wear rate ( $mm^3 N^{-1} \cdot m^{-1}$ ),  $\Delta V$  represents the

wear volume loss ( $mm^3$ ),  $F_n$  is the applied normal load (N), and  $S$  corresponds to the sliding distance (m). This method enables a quantitative comparison of the wear performance across different lubricant formulations under severe boundary lubrication conditions.

As shown in Fig. 11, the base oil (PAO8) exhibits almost the highest wear rate, highlighting its limited antiwear capability. The incorporation of nanoparticles significantly reduces wear in all tested concentrations except for the 0.05 wt %  $CeO_2-ZrO_2$  nanolubricant, which shows an unexpected increase in wear rate compared to the other nanolubricants. The best wear reduction is observed at 0.05 wt % for  $ZrO_2$  and 0.10 wt % for  $CeO_2-ZrO_2$  nanolubricant, suggesting an optimal nanoparticle concentration for effective wear protection.

The anomalous behaviour at 0.05 %  $CeO_2-ZrO_2$  could be attributed to insufficient nanoparticle availability to form a stable and protective tribofilm. At very low concentrations, nanoparticles may not fully cover the contact surface or may not effectively contribute to the rolling/sliding mechanism, leading to a lubrication regime closer to that of the base oil. Additionally, particle agglomeration at low concentrations could reduce the dispersion stability, preventing an even distribution within the lubricant film and leading to localised asperity contact and increased wear. Similar trends have been reported in nanoparticle-based lubrication studies [43,44], where an optimal concentration range exists, beyond which either insufficient coverage or excessive particle agglomeration can diminish lubrication efficiency.

Fig. 12 shows the extracted cross-sectional wear profiles for the neat PAO8 and for the nanolubricants with the highest anti-wear capacity concentrations (0.05 wt % of  $ZrO_2$  and 0.1 wt % for  $CeO_2-ZrO_2$ ), showing a clear reduction of the wear with respect to the neat base oil. The roughness ( $R_a$ ) of the wear scar was also measured with an average uncertainty of 2 nm (Table 2) to analyse the anti-wear capacity of the nanolubricants and the possible wear mechanism produced by the nanoparticles. The presence of the nanoparticles generally produces an increase in the roughness of the wear pattern. This fact allows to confirm that the polishing effect produced by the nanoparticles is not the main mechanism that justifies the AW improvement for these nanolubricants, but a repair effect or a tribo-film formation can occur [45].

The reduction in the friction coefficient (COF) and the surface are obtained in this work when  $ZrO_2$  or  $CeO_2-ZrO_2$  are used as additives of PAO8, has been compared with those previously determined by Linaera et al. [22,46] for PAO8 + ( $TiO_2$ -OA (coated with oleic acid), for PAO8 +  $CaCO_3$  (uncoated) and PAO8 +  $CeF_3$  (uncoated). As can be seen in Fig. 13a, the biggest reduction in the COF was obtained with the nanoparticles coated with oleic acid,  $TiO_2$ -OA, we must point out that in this case the PAO8 has been additivated with 0.35 wt % of  $TiO_2$ -OA but also with 0.20 wt % of oleic acid. For the uncoated nanoparticles  $ZrO_2$  or  $CeO_2-ZrO_2$   $CaCO_3$ , the reductions are quite similar, around 13 % COF reduction, but the results are slightly worse with  $CeF_3$ . On the other hand, the biggest reductions obtained for the wear area in this work with  $ZrO_2$  (73 %) are like those obtained previously [22] by using  $TiO_2$ -OA (76 %) as additive. For  $CeO_2-ZrO_2$  the wear area reduction is better than those obtained with  $CaCO_3$  and with  $CeF_3$  (Fig. 13b).

To complete the analysis of the wear reduction mechanisms of  $ZrO_2$  and  $CeO_2-ZrO_2$ , that can explain the improvement of the tribological performance, Raman microscopy studies were carried out. These measurements make possible both, to obtain a surface map within the wear tracks of the pins used, and to observe the distribution of the nanoparticles inside. Raman analysis was performed with a confocal Raman microscope at 532 nm wavelength for the wear tracks of the pins

Table 2

Average values for the surface roughness ( $R_a$ ) of the wear track lubricated with the neat PAO8 and with each nanolubricant.

Lubricant	$R_a/nm$	Lubricant	$R_a/nm$	Lubricant	$R_a/nm$
PAO8	11	+0.1 wt% $ZrO_2$	31	+0.075 wt% $CeO_2-ZrO_2$	14
+0.05 wt% $ZrO_2$	17	+0.2 wt% $ZrO_2$	18	+0.1 wt% $CeO_2-ZrO_2$	21
+0.075 wt% $ZrO_2$	61	+0.05 wt% $CeO_2-ZrO_2$	14	+0.2 wt% $CeO_2-ZrO_2$	77

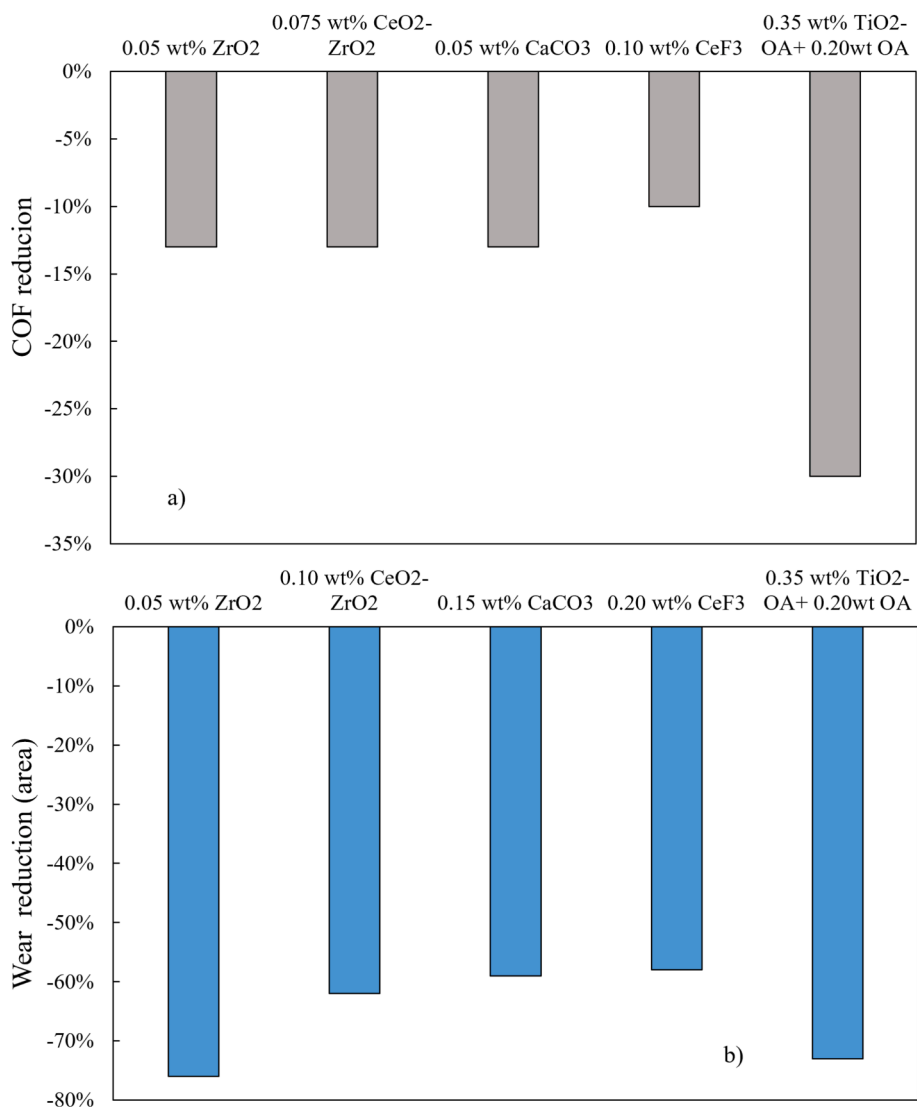


Fig. 13. Comparison of (a) the reduction in the COF and (b) the reduction in wear scar area versus previous results by Liñeira et al. [23,43] using the same base oil (PAO8).

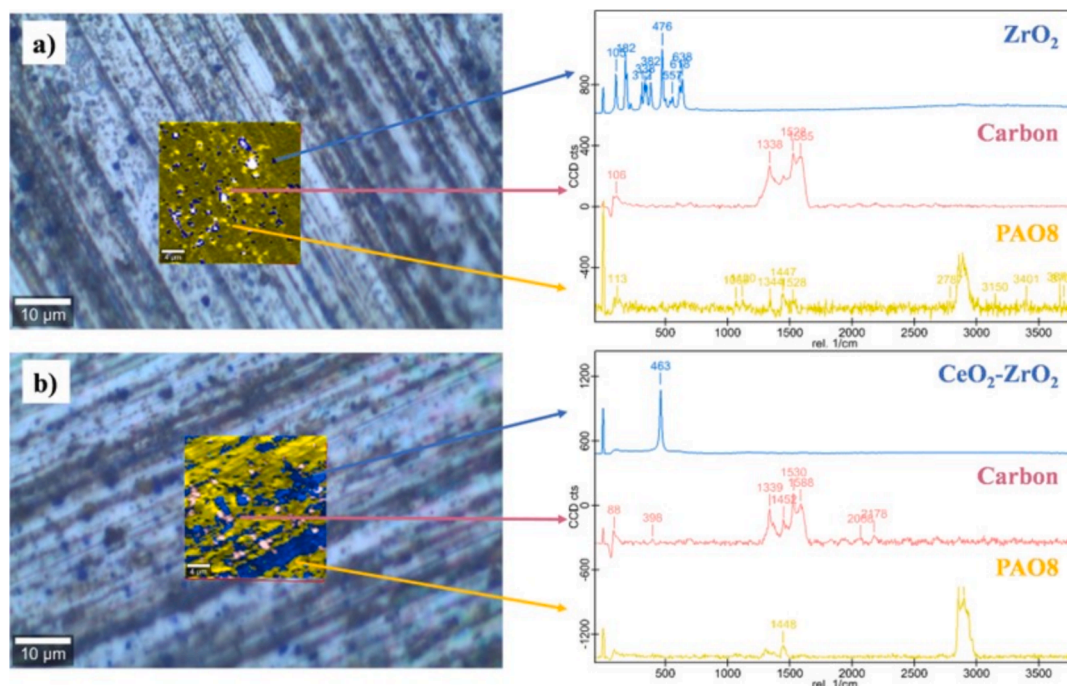


Fig. 14. Raman mapping analysis of the wear tracks of the pins lubricated with 0.05 wt%  $ZrO_2$  (a) and with 0.1 wt%  $CeO_2-ZrO_2$  (b) both in PAO8.

lubricated with the optimum concentrations of anti-wear capacity (0.05 wt%  $ZrO_2$  and 0.1 wt% of  $CeO_2-ZrO_2$ ). Raman spectra corresponding to neat PAO8 and to  $ZrO_2$  and  $CeO_2-ZrO_2$  nanoparticles were already presented in Fig. 1 and Fig. 4, respectively. As can be seen in Fig. 14, the grooves produced during the friction tests are clearly visible in the sliding direction along which an accumulation of PAO8 lubricant can be observed. In addition, the characteristic stripes of each nanoadditive have been detected in the wear tracks of the lubricated pins. Fig. 14a shows the analysis performed for the wear track generated on the steel surface of the contact lubricated with PAO8/ $ZrO_2$  (0.05 wt%). Indeed, PAO8 is mostly spread over almost the entire surface of the contact lubricated steel and  $ZrO_2$  nanoparticles (blue colour) are lodged along the wear track in the sliding direction.

As shows Fig. 14b, for the contact lubricated with PAO8/ $CeO_2-ZrO_2$  (0.1 wt%), a predominant presence of PAO8, (yellow colour) is observed, although the presence of the nanoadditive ( $CeO_2-ZrO_2$ ) is also clear in the form of continuous tribo-films (blue colour). Traces of carbon have been detected on both surfaces analysed (pink colour). These carbon deposits are generated during friction tests due to the abrasion to which the steel is subjected, as previously pointed out by Nasser et al [47]. Therefore, the detection of both nanoadditives in the wear traces is evidence that the improved lubricating ability of the nanolubricants is due to the film-forming mechanism of the nanoparticles on the sliding surfaces, thus improving the tribological properties (friction and wear) of the base oil.

SEM observations, shown in Fig. 15, have been carried out at two different magnifications, 500 and 5000 $\times$  for the steel pins lubricated with plain PAO8 base oil, with 0.05 wt%  $ZrO_2$ /PAO8 and with 0.1 wt%  $CeO_2-ZrO_2$ /PAO8 nanolubricants. In 500 X images (Fig. 15 a, c and e),

the entire wear track generated on the steel pins lubricated can be observed. Thus, minor wear is revealed for the contact lubricated with 0.05 wt%  $ZrO_2$ , which coincides with the reported results in Table 1 and Fig. 12. The worn surface lubricated with  $ZrO_2$ -nanolubricant, i.e. Fig. 15(d), shows small pitting, which could be attributed to adhesive wear. Whereas when the contact is lubricated with  $CeO_2-ZrO_2$  nanolubricant Fig. 15(f), deep elongated grooves along the sliding direction can be observed, which are formed as a product of abrasive wear [48]. This is consistent with the roughness measurements (Table 2). Thus, the type of wear produced varies depending on the nanoadditive used. The excellent anti-wear behaviour and friction effect using nanolubricants are closely related to the presence of  $ZrO_2$  nanoparticles on the wear surface, which was verified by energy dispersive X-ray spectrometry (EDX). Table 3 shows the increase in elemental Zr content in the worn tracks lubricated with both nanolubricants. It can be stated that the Zr nanoparticles have been entrained on contact and interacted with the surface, leading to an improvement in the tribological behaviour of the base oil. However, the presence of Ce could not be detected in the contact. The most likely anti-wear mechanism of the nanoparticulate additive is the formation of a protective layer due to the welding of the nanoparticles onto the wear surface (tribosintering), which has been confirmed with Raman mapping (Fig. 14). In addition, the spherical morphology of the nanoparticles used can perform the rolling mechanism, whereby the nanoparticles act as nano-bearings between the contact surfaces [49].

## 5. Conclusions

In this work, experimental thermophysical and tribological

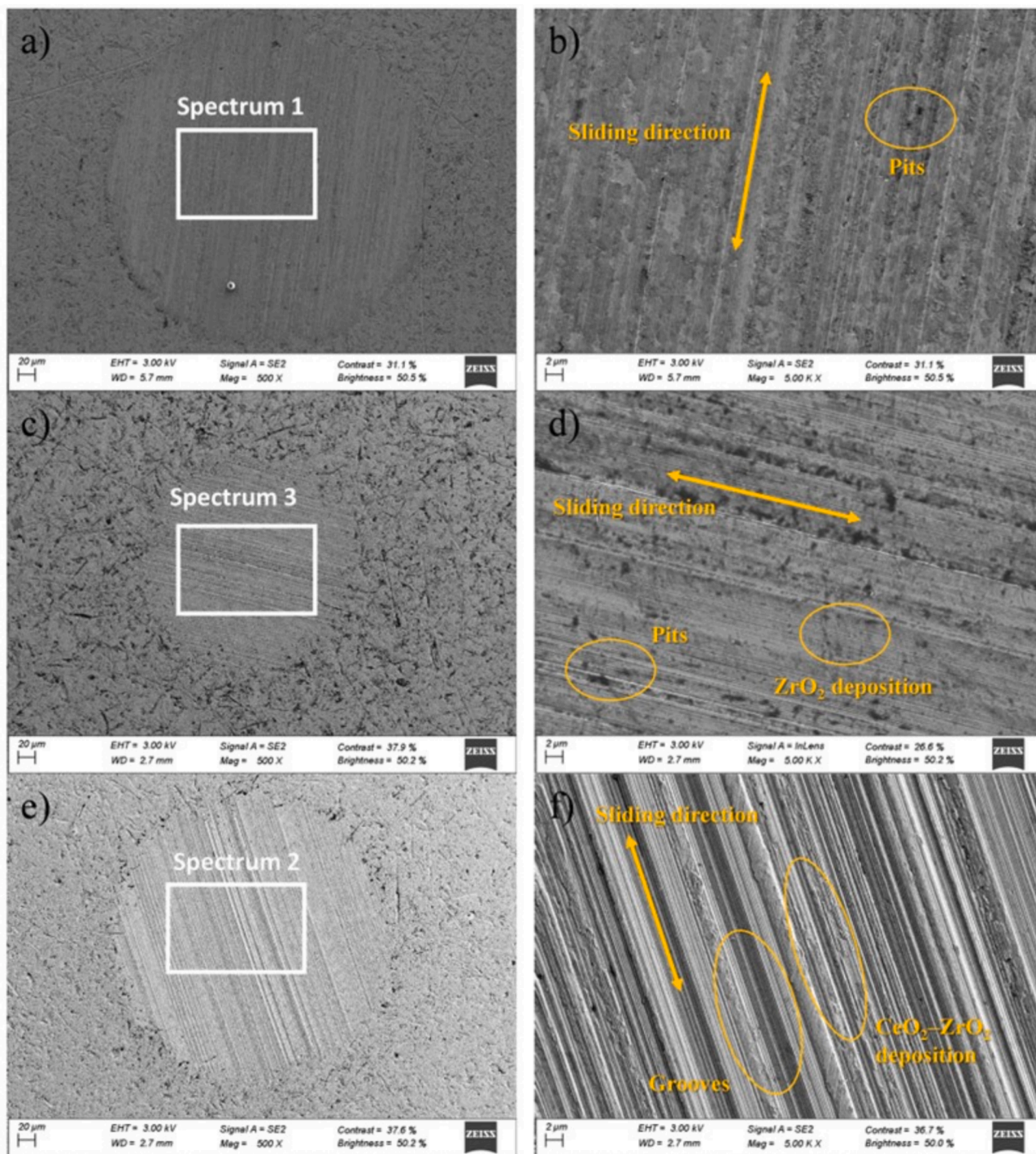


Fig. 15. SEM images inside of the wear scars on the steel pins from the test lubricated with: a) PAO8 (500 X), b) PAO8 (5000 X), c) PAO8 with 0.05 wt% ZrO<sub>2</sub> (500 X), d) PAO8 with 0.05 wt% ZrO<sub>2</sub> (5000 X), e) PAO8 with 0.1 wt% CeO<sub>2</sub>-ZrO<sub>2</sub> (500 X) and f) PAO8 with 0.1 wt% CeO<sub>2</sub>-ZrO<sub>2</sub> (5000 X).

**Table 3**

EDX analysis of worn surface of steel pins tested with PAO8 base oil, 0.1 wt% CeO<sub>2</sub>-ZrO<sub>2</sub> and 0.05 wt% ZrO<sub>2</sub> nanolubricants.

Elemental composition	Steel AISI 52100/ Spectrum 1	0.1 wt% CeO <sub>2</sub> - ZrO <sub>2</sub> /Spectrum 3	0.05 wt% ZrO <sub>2</sub> / Spectrum 2
C	7.26	6.85	5.28
O	1.75	1.41	1.24
Mg	0.15	—	—
Al	0.60	0.18	0.12
Si	0.28	0.27	0.29
S	0.02	0.03	0.01
Cr	1.43	1.41	1.45
Mn	0.41	0.43	0.45
Fe	87.87	89.04	90.57
Zr	0.23	0.39	0.58
Total	100	100	100

properties were determined for PAO8 additivated with zirconia and hybrid ceria-zirconia nanoparticles at concentrations from 0.05 wt% to 0.2 wt%. The main findings of this study are:

- The presence of zirconia and hybrid ceria-zirconia does not affect the volumetric behaviour of the base oil, however, an increase in the viscosity up to 13 % is observed.
- The addition of ZrO<sub>2</sub> (0.05 wt%) or CeO<sub>2</sub>-ZrO<sub>2</sub> (0.075 wt%) nanoparticles decreases the friction coefficient of PAO8 neat oil around 13 % under boundary lubrication conditions.
- ZrO<sub>2</sub> nanoadditives remove any abrasion or deformation of the surface: reduction of 66 % in the wear depth with respect to the neat base oil.
- The tribo-film formation and rolling effect produced by both types of spherical additives justify the improvement in the tribological behaviour.

#### CRediT authorship contribution statement

**María J.G. Guimarey:** Writing – review & editing, Writing – original draft, Validation, Resources, Methodology, Investigation, Conceptualization. **Arturo Castro Currás:** Methodology, Investigation. **José M. Linaera Del Río:** Writing – review & editing, Writing – original draft, Validation, Methodology, Investigation. **María J.P. Comuñas:** Writing – review & editing, Supervision, Funding acquisition.

#### Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

#### Acknowledgements

This research is supported by projects PID2020-112846RB-C22 and ED431C 2024/06 funded by MCIN/AEI/10.13039/501100011033 and through the Xunta de Galicia, respectively. The authors would like to thank the use of RIAIDT-USC analytical facilities. Dr M.J.G.G. and Dr. J. M.L.dR are grateful for financial support through the grant reference ED481D 2023/016 from Xunta de Galicia (Spain) and the Margarita Salas programme, funded by MCIN/AEI/10.13039/501100011033 and “NextGenerationEU/PRTR”, respectively.

#### Appendix A. Supplementary data

Supplementary data to this article can be found online at <https://doi.org/10.1016/j.molliq.2025.127502>.

#### Data availability

Data will be made available on request.

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